

# Co-expression analysis of RNA-seq data

Andrea Rau

July 19, 2016 @ SPS Summer School



**Summer School 2016**

July 17<sup>th</sup> to 22<sup>nd</sup> 2016

« From gene expression to genomic network »

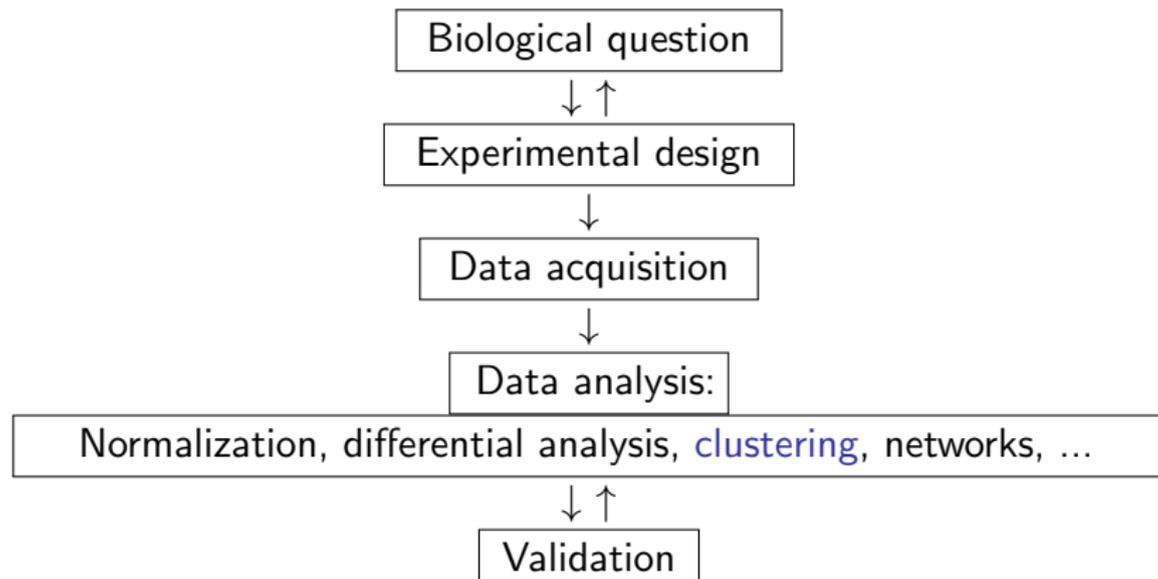
# Outline

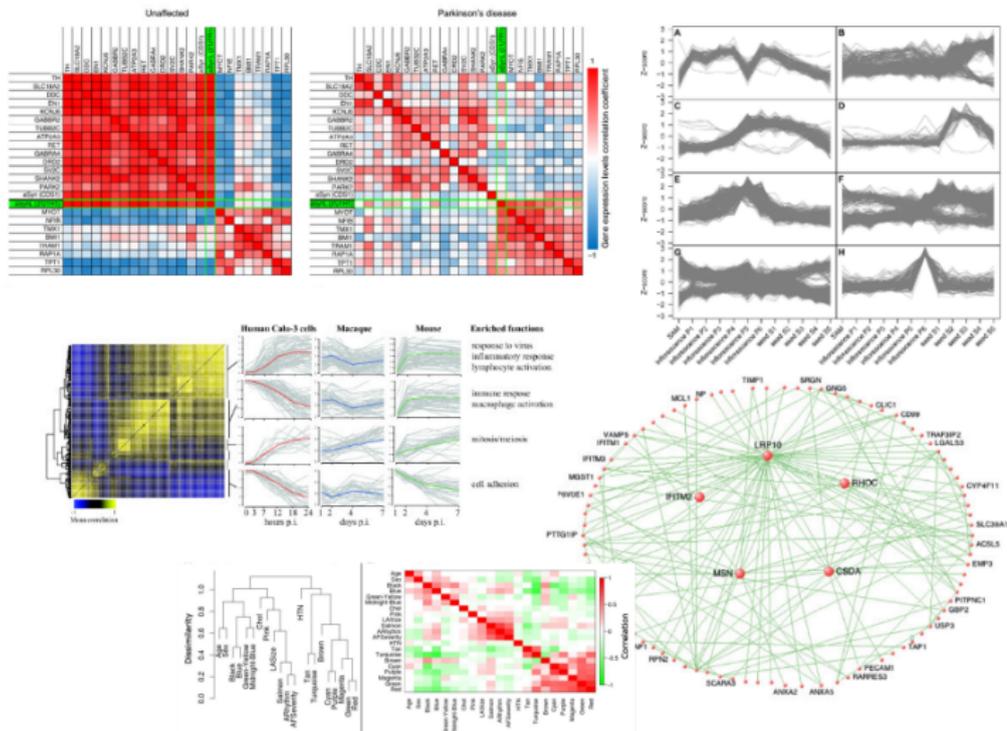
- 1 Co-expression analysis introduction
- 2 Unsupervised clustering
  - Centroid-based clustering: K-means, HCA
  - Model-based clustering
  - Mixture models for RNA-seq data
- 3 Conclusion / discussion

## Aims for this afternoon

- What is the biological/statistical meaning of co-expression for RNA-seq?
- What methods exist for performing co-expression analysis?
- How to choose the number of clusters present in data?
- Advantages / disadvantages of different approaches: speed, stability, robustness, interpretability, model selection, ...

# Design of a transcriptomics project



Gene co-expression<sup>1</sup>

<sup>1</sup>Google image search: "Coexpression"

# Gene co-expression is...

- The **simultaneous expression** of two or more genes<sup>2</sup>
- Groups of **co-transcribed** genes<sup>3</sup>
- **Similarity of expression**<sup>4</sup> (correlation, topological overlap, mutual information, ...)
- Groups of genes that have **similar expression patterns**<sup>5</sup> over a range of different experiments

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<sup>2</sup><https://en.wiktionary.org/wiki/coexpression>

<sup>3</sup><http://bioinfow.dep.usal.es/coexpression>

<sup>4</sup><http://coexpresdb.jp/overview.shtml>

<sup>5</sup>Yeung *et al.* (2001)

<sup>6</sup>Eisen *et al.* (1998)

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- **Similarity of expression**<sup>4</sup> (correlation, topological overlap, mutual information, ...)
- Groups of genes that have **similar expression patterns**<sup>5</sup> over a range of different experiments
  
- Related to shared regulatory inputs, functional pathways, and biological process(es)<sup>6</sup>

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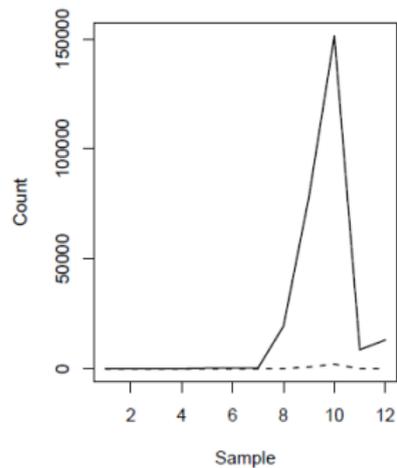
# From gene co-expression to gene function prediction

- Transcriptomic data: main source of 'omic information available for living organisms
  - Microarrays (~1995 - )
  - High-throughput sequencing: RNA-seq (~2008 - )

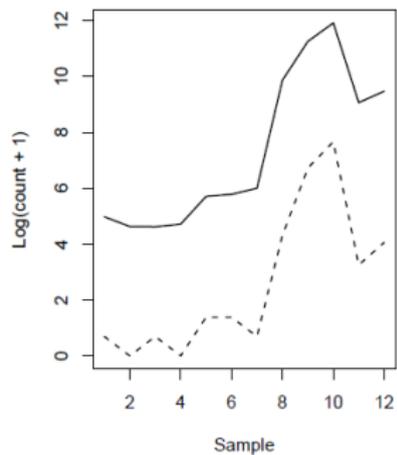
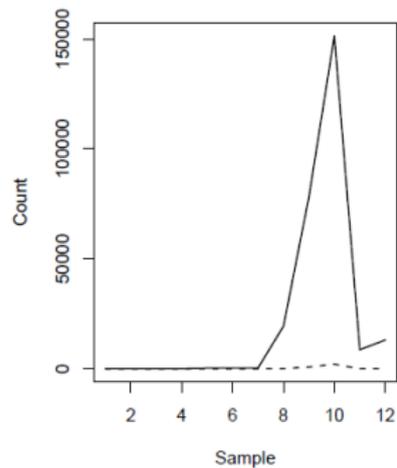
## Co-expression (clustering) analysis

- Study patterns of relative gene expression (*profiles*) across several conditions
- $\Rightarrow$  Co-expression is a tool to study genes without known or predicted function (orphan genes)
- Exploratory tool to identify expression trends from the data ( $\neq$  sample classification, identification of differential expression)

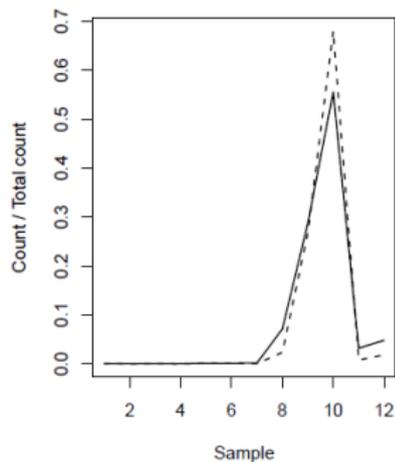
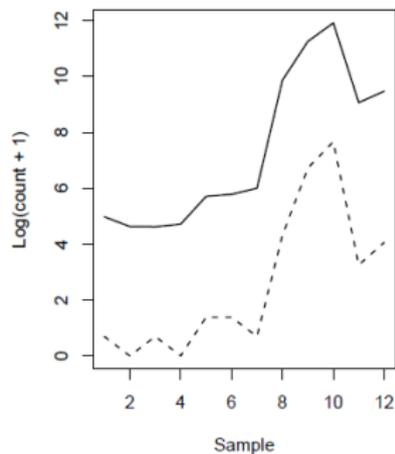
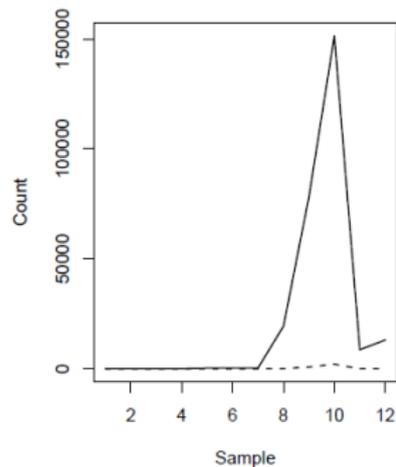
# RNA-seq profiles for co-expression



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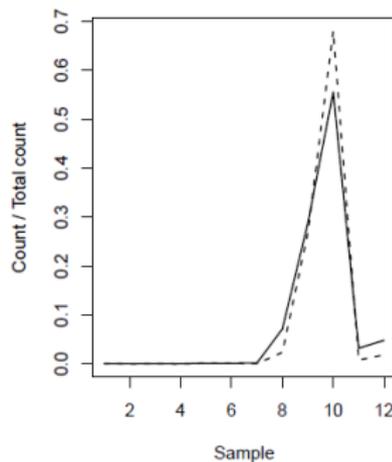
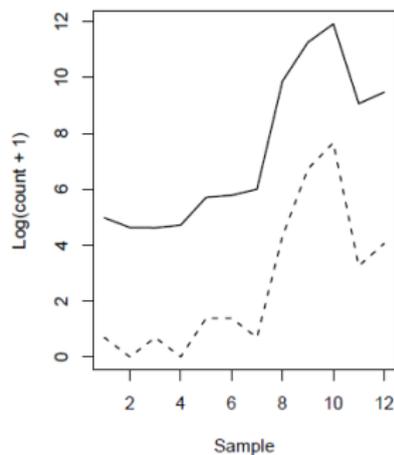
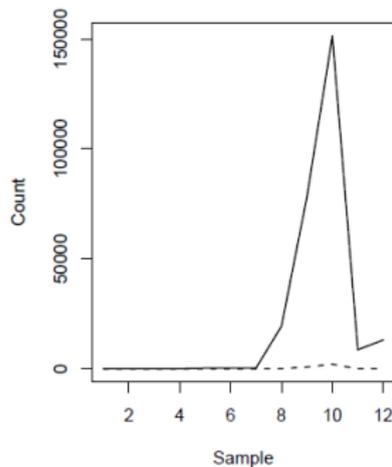


# RNA-seq profiles for co-expression



- Let  $y_{ij}$  be the raw count for gene  $i$  in sample  $j$ , with library size  $s_j$
- Profile for gene  $i$ :  $p_{ij} = \frac{y_{ij}}{\sum_{\ell} y_{i\ell}}$

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- Profile for gene  $i$ :  $p_{ij} = \frac{y_{ij}}{\sum_l y_{il}}$
- Normalized profile for gene  $i$ :  $p_{ij} = \frac{y_{ij}/s_j}{\sum_l y_{il}/s_j}$

# Unsupervised clustering

## Objective

Define **homogeneous** and **well-separated** groups of genes from transcriptomic data

What does it mean for a pair of genes to be **close**?  
Given this, how do we define **groups**?

# Unsupervised clustering

## Objective

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What does it mean for a pair of genes to be **close**?  
Given this, how do we define **groups**?

Two broad classes of methods typically used:

- 1 Centroid-based clustering (K-means and hierarchical clustering)
- 2 Model-based clustering (mixture models)

# Outline

- 1 Co-expression analysis introduction
- 2 **Unsupervised clustering**
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# Similarity measures

Similarity between genes is defined with a distance:

- **Euclidian distance** (L2 norm):  $d^2(\mathbf{y}_i, \mathbf{y}_{i'}) = \sum_{\ell=1}^p (y_{i\ell} - y_{i'\ell})^2$   
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⇒ Note: sensitive to scaling and differences in average expression level
- Pearson correlation coefficient:  $d_{pc}(\mathbf{y}_i, \mathbf{y}_{i'}) = 1 - \rho_{i,i'}$
- Spearman rank correlation coefficient: as above but replace  $y_{ij}$  with rank of gene  $i$  across all samples  $j$
- Absolute or squared correlation:  $d_{ac}(\mathbf{y}_i, \mathbf{y}_{i'}) = 1 - |\rho_{i,i'}|$  or  $d_{sc}(\mathbf{y}_i, \mathbf{y}_{i'}) = 1 - \rho_{i,i'}^2$
- Mahalanobis distance:  $d_{\text{Mahalanobis}}(\mathbf{y}_i, \mathbf{y}_{i'}) = (\mathbf{y}_i - \mathbf{y}_{i'})' \Sigma^{-1} (\mathbf{y}_i - \mathbf{y}_{i'})$
- Manhattan distance:  $d_{\text{Manhattan}}(\mathbf{y}_i, \mathbf{y}_{i'}) = \sum_{\ell=1}^p |y_{i\ell} - y_{i'\ell}|$

# Inertia measures

Homogeneity of a group is defined with an **inertia criterion**:

- Let  $\mathbf{y}_G$  be the centroid of the dataset and  $\mathbf{y}_{C_k}$  the centroid of group  $C_k$

$$\begin{aligned}\text{Inertia} &= \sum_{i=1}^n d^2(\mathbf{y}_i, \mathbf{y}_G) \\ &= \sum_{k=1}^K \sum_{i \in C_k} d^2(\mathbf{y}_i, \mathbf{y}_{C_k}) + \sum_{k=1}^K n_k d^2(\mathbf{y}_{C_k}, \mathbf{y}_G) \\ &= \text{within-group inertia} + \text{between-group inertia}\end{aligned}$$

# In practice...

Objective: cluster  $n$  genes into  $K$  groups,  
maximizing the between-group inertia

- Exhaustive search is impossible
- Two algorithms are often used
  - 1 K-means
  - 2 Hierarchical clustering

# K-means algorithm

**Initialization**  $K$  centroids are chosen randomly or by the user

## Iterative algorithm

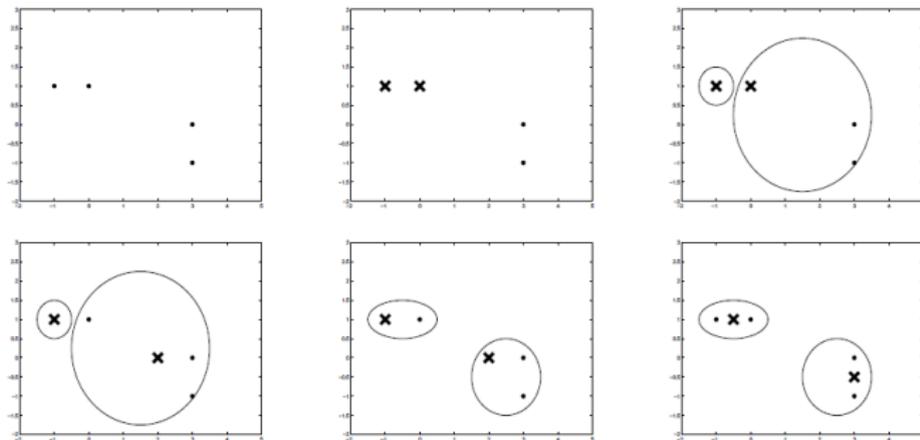
- 1 **Assignment** Each gene is assigned to a group according to its distance to the centroids.
- 2 **Calculation of the new centroids**

**Stopping criterion:** when the maximal number of iterations is achieved OR when groups are stable

## Properties

- Rapid and easy
- Results depend strongly on initialization
- Number of groups  $K$  is fixed a priori

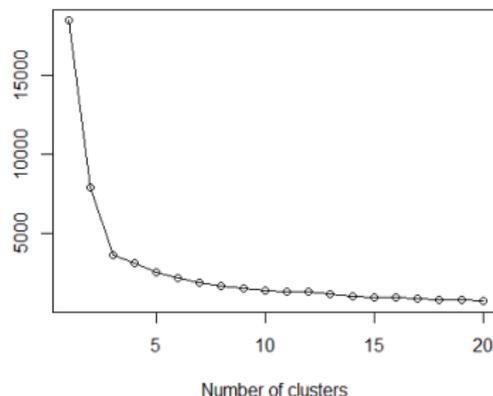
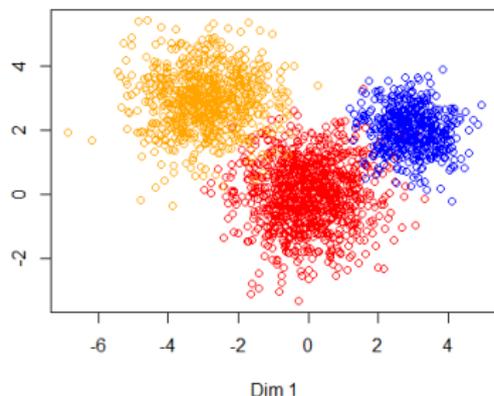
# K-means illustration



Animation: <http://shabal.in/visuals/kmeans/1.html>

# K-means algorithm: Choice of $K$ ?

- Elbow plot of within-sum of squares: examine the percentage of variance explained as a function of the number of clusters



- Gap statistic: estimate change in within-cluster dispersion compared to that under expected reference null distribution
- Silhouette statistic: measure of how closely data within a cluster is matched and how loosely it is matched to neighboring clusters

# Hierarchical clustering analysis (HCA)

**Objective** Construct embedded partitions of  $(n, n - 1, \dots, 1)$  groups, forming a tree-shaped data structure (dendrogram)

## Algorithm

- **Initialization**  $n$  groups for  $n$  genes
- **At each step:**
  - **Closest** genes are clustered
  - Calculate **distance** between this new group and the remaining genes

# Distances between groups for HCA

## Distances between groups

- Single-linkage clustering:

$$D(C_k, C_{k'}) = \min_{x \in C_i} \min_{x' \in C_{i'}} d^2(x, x')$$

- Complete-linkage clustering:

$$D(C_k, C_{k'}) = \max_{x \in C_i} \max_{x' \in C_{i'}} d^2(x, x')$$

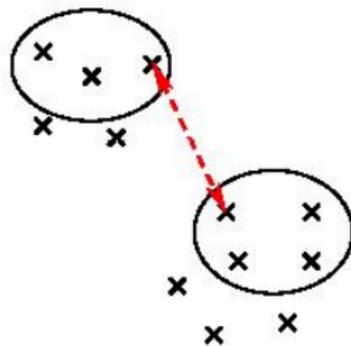
- Ward distance:

$$D(C_k, C_{k'}) = d^2(x_{C_k}, x_{C_{k'}}) \times \frac{n_k n_{k'}}{n_k + n_{k'}}$$

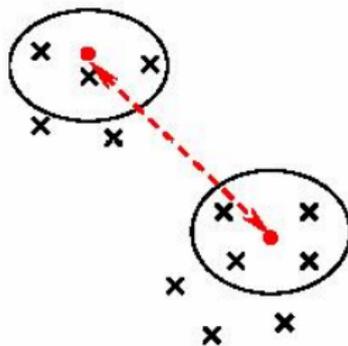
where  $n_k$  is the number of genes in group  $C_k$

# Distances between groups for HCA

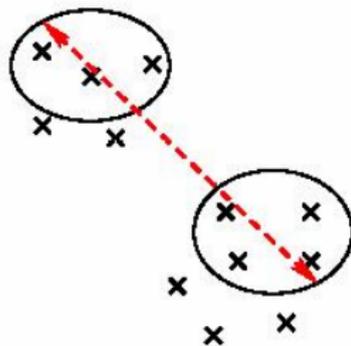
- Simple linkage



- Average linkage



- Complete linkage

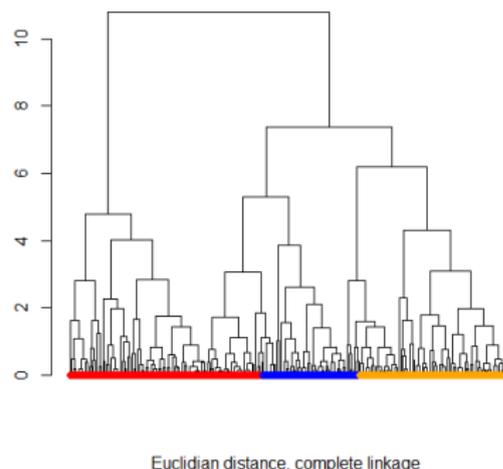
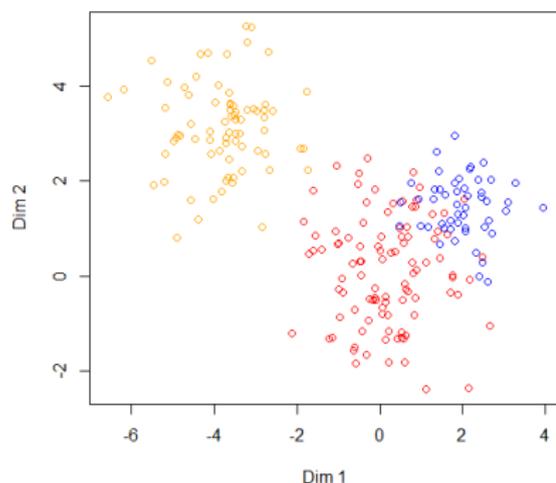


Source: <http://compbio.pbworks.com/w/page/16252903/Microarray%20Clustering%20Methods%20and%20Gene%20Ontology>

# HCA: additional details

## Properties:

- HCA is stable since there is no initialization step
- $K$  is chosen according to the tree
- Results strongly depend on the chosen distances
- Branch lengths are proportional to the percentage of inertia loss  $\Rightarrow$  a long branch indicates that the 2 groups are not homogeneous



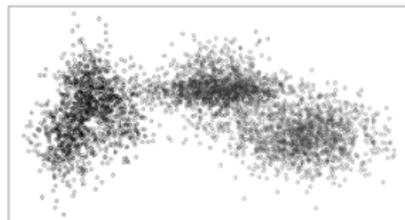
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# Model-based clustering

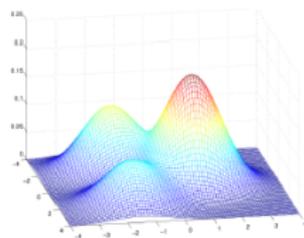
- Probabilistic clustering models : data are assumed to come from distinct subpopulations, each modeled separately
- Rigorous framework for parameter estimation and model selection
- **Output**: each gene assigned a probability of cluster membership

what we observe

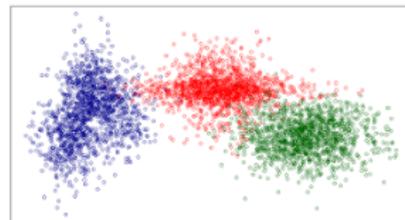


$Z = ?$

the model



the expected results



$Z : 1 = \bullet, 2 = \bullet, 3 = \bullet$

# Key ingredients of a mixture model

- Let  $\mathbf{y} = (\mathbf{y}_1, \dots, \mathbf{y}_n)$  denote the observations with  $\mathbf{y}_i \in \mathbb{R}^p$
- We introduce a latent variable to indicate the group from which each observation arises:

$$Z_i \sim \mathcal{M}(n; \pi_1, \dots, \pi_K),$$

$$P(Z_i = k) = \pi_k$$

- Assume that  $\mathbf{y}_i$  are conditionally independent given  $Z_i$
- Model the distribution of  $\mathbf{y}_i|Z_i$  using a parametric distribution:

$$(\mathbf{y}_i|Z_i = k) \sim f(\cdot; \theta_k)$$

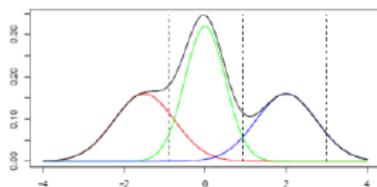
# Questions around the mixtures

- **Model:** what distribution to use for each component ?  
↪ depends on the observed data.
- **Inference:** how to estimate the parameters ?  
↪ usually done with an EM-like algorithm (Dempster *et al.*, 1977)
- **Model selection:** how to choose the number of components ?
  - A collection of mixtures with a **varying number of components** is usually considered
  - A **penalized criterion** is used to select the best model from the collection

# Clustering data into components

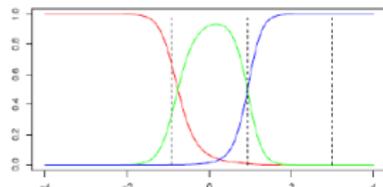
Distributions:

$$g(x) = \pi_1 f_1(x) + \pi_2 f_2(x) + \pi_3 f_3(x)$$



Conditional probabilities:

$$\tau_{ik} = \frac{\pi_k f_k(x_i)}{g(x_i)}$$



Maximum a posteriori (MAP) rule: Assign genes to the component with highest conditional probability  $\tau_{ik}$ :

$\tau_{ik}$ (%)	$k = 1$	$k = 2$	$k = 3$
$i = 1$	65.8	34.2	0.0
$i = 2$	0.7	47.8	51.5
$i = 3$	0.0	0.0	100
...	...	...	...

# Model selection for mixture models

Asymptotic penalized criteria<sup>7</sup>

- **BIC** aims to identify the best model  $K$  wrt the **global fit** of the data distribution:

$$BIC(K) = -\log P(\mathbf{y}|K, \hat{\theta}_K) + \frac{\nu_K}{2} \log(n)$$

where  $\nu_K$  is the # of free parameters and  $\hat{\theta}_K$  is the MLE of the model with  $K$  clusters

- **ICL** aims to identify the best model  $K$  wrt **cluster separation**:

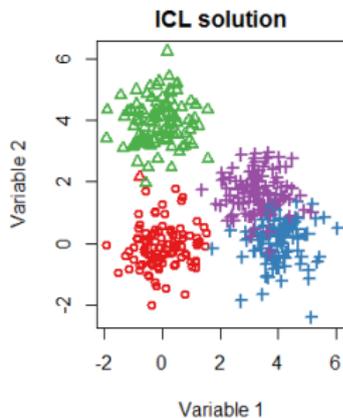
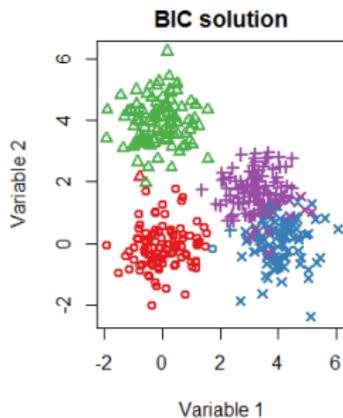
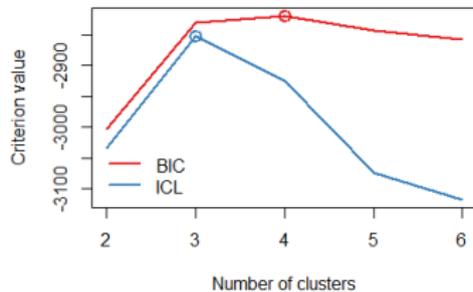
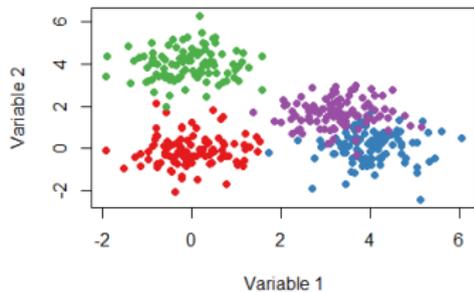
$$ICL(K) = BIC(K) + \left( - \sum_{i=1}^n \sum_{k=1}^K \tau_{ik} \log \tau_{ik} \right)$$

⇒ Select  $K$  that **minimizes** BIC or ICL (but be careful about their sign!)

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<sup>7</sup>Asymptotic: approaching a given value as the number of observations  $n \rightarrow \infty$

# Model selection for mixture models: BIC vs ICL



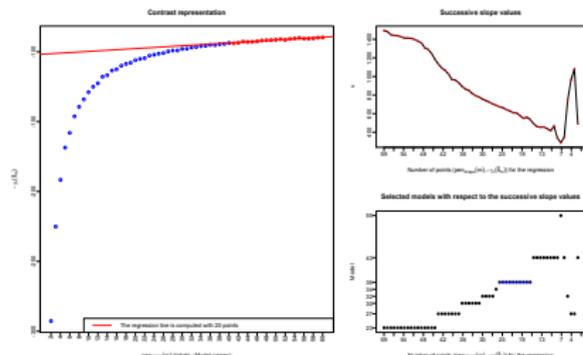
# Model selection for mixture models

## Non-asymptotic penalized criteria

Recent work has been done in a non-asymptotic context using the slope heuristics (Birgé & Massart, 2007):

$$SH(K) = \log P(\mathbf{y}|K, \hat{\theta}_K) + \kappa \text{pen}_{shape}(K)$$

- In large dimensions, linear behavior of  $\frac{D}{n} \mapsto -\gamma_n(\hat{S}_D)$
- Estimation of slope to calibrate  $\hat{\kappa}$  in a data-driven manner (Data-Driven Slope Estimation = DDSE), capushe R package



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# Finite mixture models for RNA-seq

Assume data  $\mathbf{y}$  come from  $K$  distinct subpopulations, each modeled separately:

$$f(\mathbf{y}|K, \Psi_K) = \prod_{i=1}^n \sum_{k=1}^K \pi_k f_k(\mathbf{y}_i; \theta_k)$$

- $\boldsymbol{\pi} = (\pi_1, \dots, \pi_K)'$  are the mixing proportions, where  $\sum_{k=1}^K \pi_k = 1$
- $f_k$  are the densities of each of the components

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- $f_k$  are the densities of each of the components
- For microarray data, we often assume  $\mathbf{y}_i|k \sim \text{MVN}(\boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k)$
- What about RNA-seq data?

# Finite mixture models for RNA-seq data

$$f(\mathbf{y}|K, \boldsymbol{\Psi}_K) = \prod_{i=1}^n \sum_{k=1}^K \pi_k f_k(\mathbf{y}_i|\boldsymbol{\theta}_k)$$

For RNA-seq data, we must choose the family & parameterization of  $f_k(\cdot)$ :

- 1 Directly model read counts (HTSCluster):

$$\mathbf{y}_i|Z_i = k \sim \prod_{j=1}^J \text{Poisson}(y_{ij}|\mu_{ijk})$$

- 2 Apply appropriately chosen data transformation (coseq):

$$g(\mathbf{y}_i)|Z_i = k \sim \text{MVN}(\boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k)$$

# Poisson mixture models for RNA-seq (Rau *et al.*, 2015)

$$\mathbf{y}_i | Z_i = k \sim \prod_{j=1}^J \text{Poisson}(y_{ij} | \mu_{ijk})$$

**Question:** How to parameterize the mean  $\mu_{ijk}$  to obtain meaningful clusters of co-expressed genes?

# Poisson mixture models for RNA-seq (Rau *et al.*, 2015)

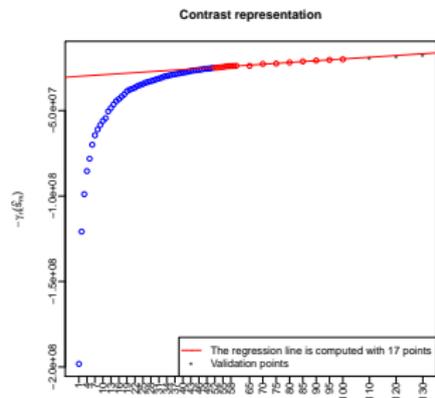
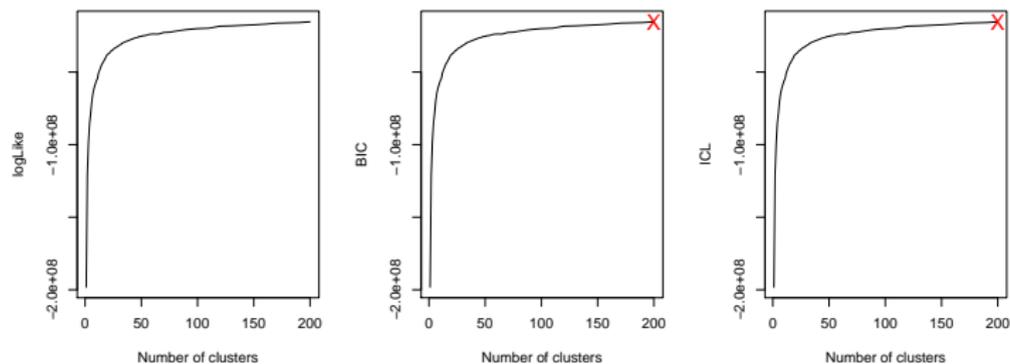
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**Question:** How to parameterize the mean  $\mu_{ijk}$  to obtain meaningful clusters of co-expressed genes?

$$\mu_{ijk} = w_i \lambda_{jk} s_j$$

- $w_i$  : overall **expression level** of observation  $i$  ( $y_i$ .)
- $\lambda_k = (\lambda_{jk})$  : clustering parameters that define the **profiles of genes** in cluster  $k$  (variation around  $w_i$ )
- $s_j$  : **normalized library size** for sample  $j$ , where  $\sum_j s_j = 1$

# Behavior of model selection in practice for RNA-seq



# Discussion of PMM for RNA-seq data

## Advantages:

- 1 Directly models counts (no data transformation necessary)
- 2 Clusters interpreted in terms of profiles around mean expression
- 3 Implemented in HTSCluster package on CRAN (v1.0.8)
- 4 Promising results on real data...

# Discussion of PMM for RNA-seq data

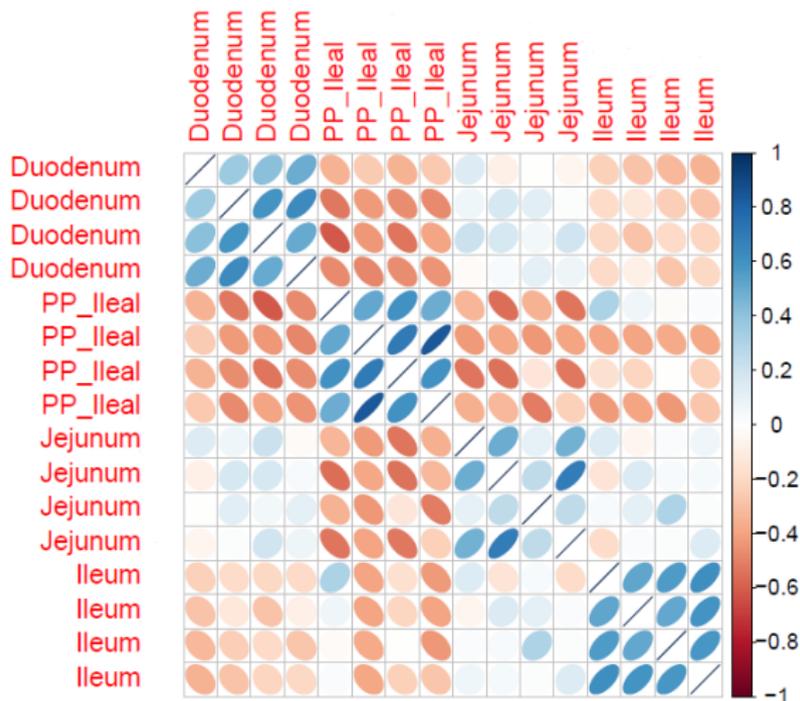
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## Limitations:

- 1 Slope heuristics requires a very large collection of models to be fit
- 2 Restrictive assumption of **conditional independence** among samples
- 3 Cannot model **per-cluster correlation** structures
- 4 Poisson distribution requires assuming that **mean = variance**

# Correlation structures in RNA-seq data



Example: data from Mach *et al.* (2014) on site-specific gene expression along the gastrointestinal tract of 4 healthy piglets

# Gaussian mixture models for RNA-seq

Idea: Transform RNA-seq data, then apply Gaussian mixture models

Several data transformations have been proposed for RNA-seq to render the data approximately homoskedastic:

- $\log_2(y_{ij} + c)$
- Variance stabilizing transformation (DESeq)
- Moderated log counts per million (edgeR)
- Regularized log-transformation (DESeq2)

... but recall that we wish to cluster the **normalized profiles**  $p_{ij} = \frac{y_{ij}/s_j}{\sum_{\ell} y_{i\ell}/s_j}$

## Remark: transformation needed for normalized profiles

- Note that the normalized profiles are *compositional data*, i.e. the sum for each gene  $p_{i.} = 1$
- This implies that the vector  $\mathbf{p}_i$  is linearly dependent  $\Rightarrow$  imposes constraints on the covariance matrices  $\Sigma_k$  that are problematic for the general GMM
- As such, we consider a transformation on the normalized profiles to break the sum constraint:

$$\tilde{p}_{ij} = g(p_{ij}) = \arcsin(\sqrt{p_{ij}})$$

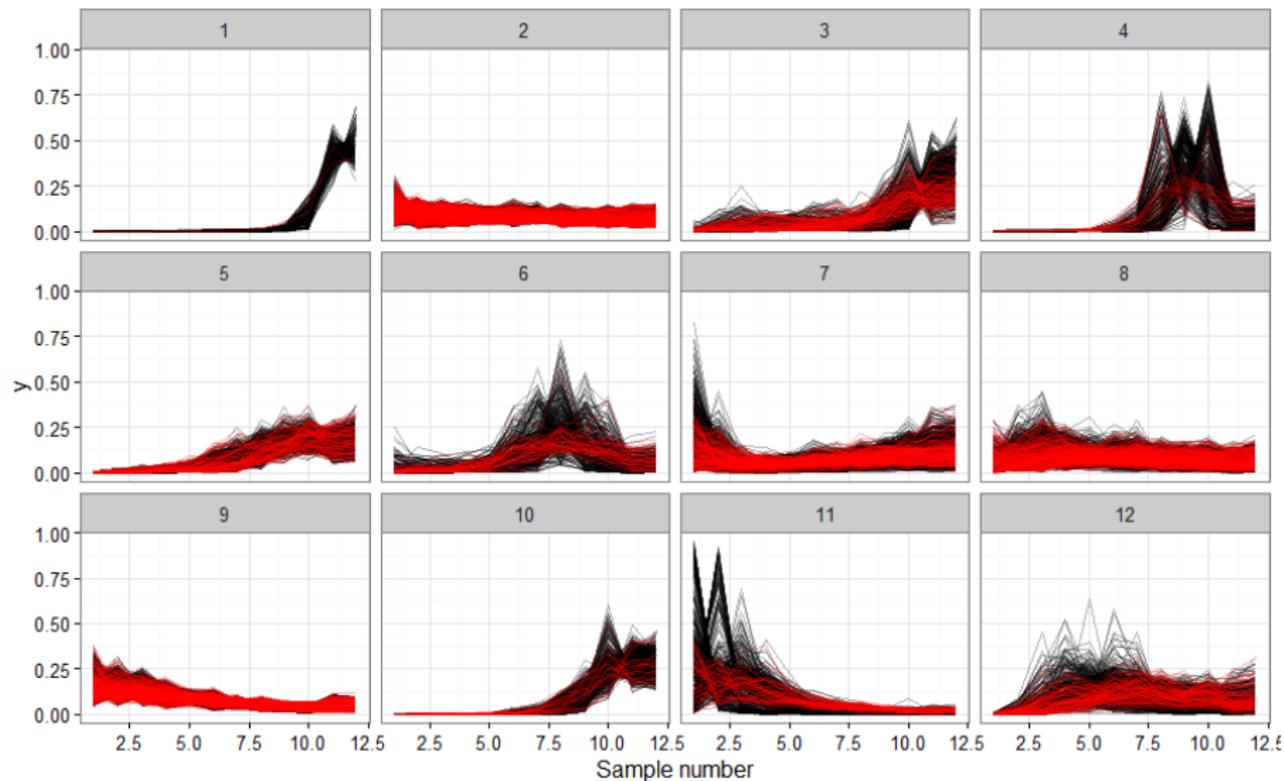
And fit a GMM to the transformed normalized profiles:

$$f(\tilde{\mathbf{p}}|K, \Psi_K) = \prod_{i=1}^n \sum_{k=1}^K \pi_k \phi(\tilde{\mathbf{p}}_i | \boldsymbol{\theta}_k, \Sigma_k)$$

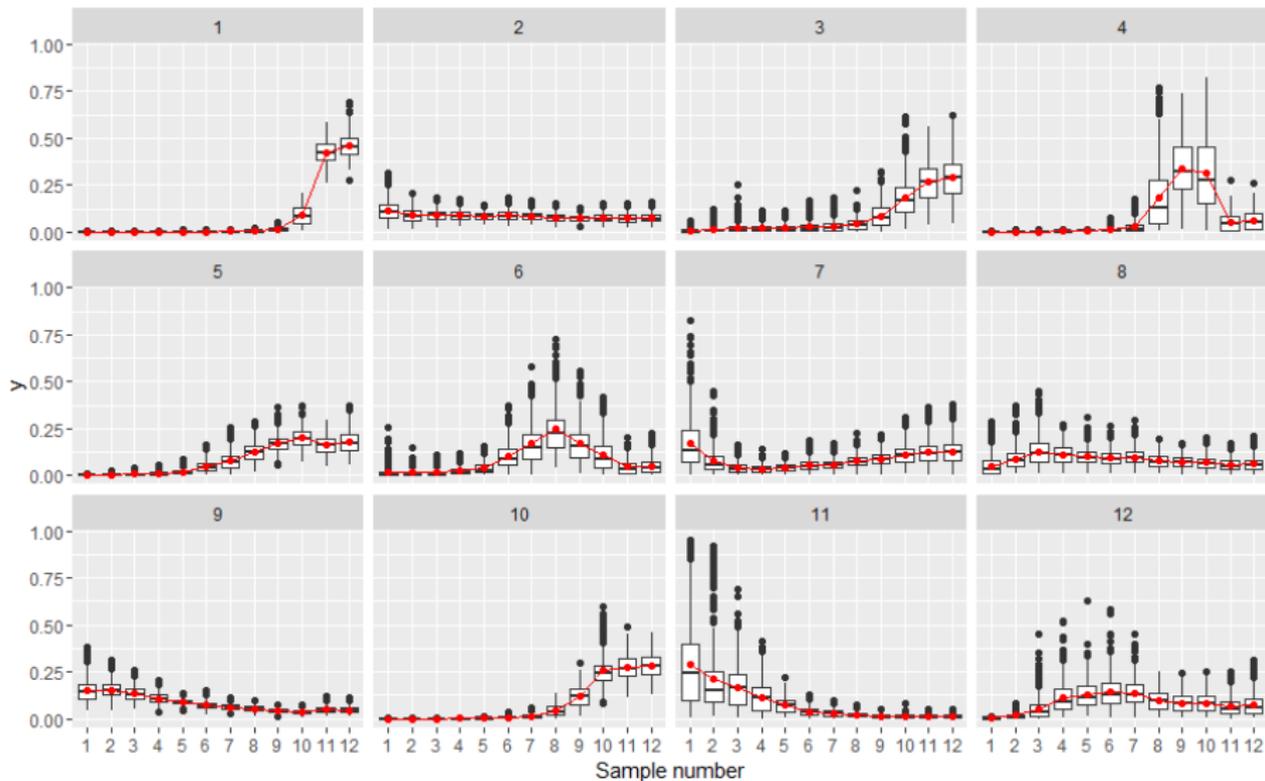
# Running the PMM or GMM for RNA-seq data with coseq

```
> library(coseq)
>
> GMM <- coseq(counts, K=2:10, model="Normal",
>               transformation="arcsin")
> summary(GMM)
> plot(GMM)
>
> ## Note: indirectly calls HTSCluster for PMM
> PMM <- coseq(counts, K=2:10, model="Poisson",
>               transformation="none")
> summary(PMM)
> plot(PMM)
```

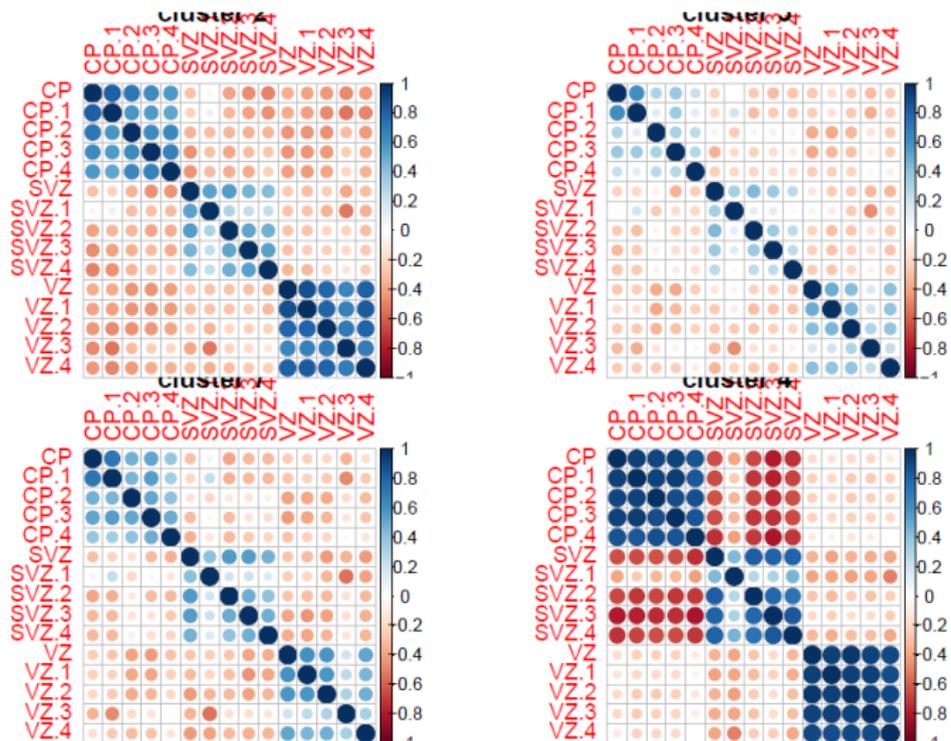
# Examining GMM results



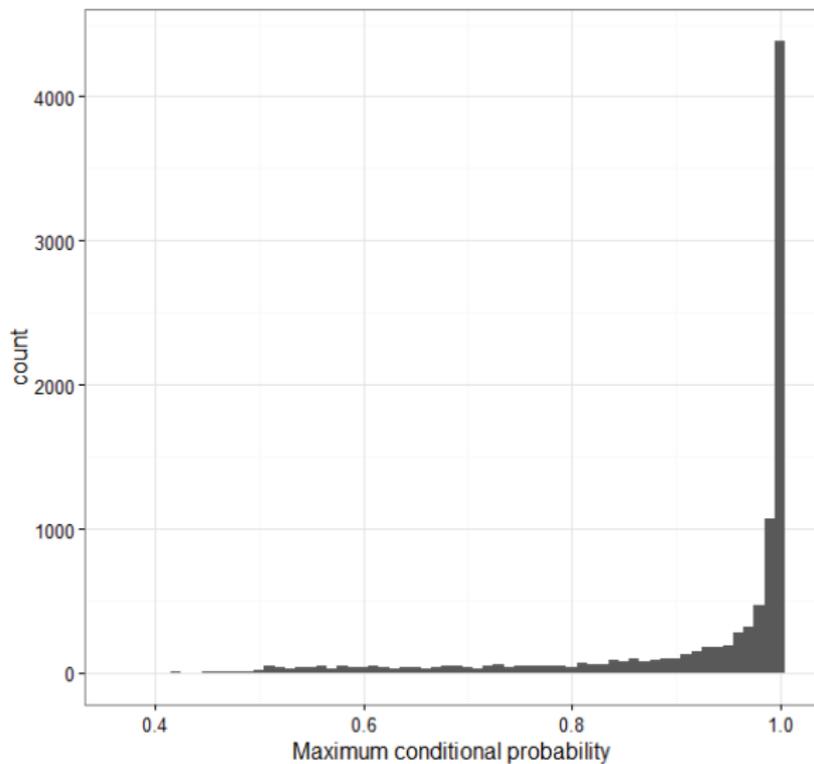
# Examining GMM results



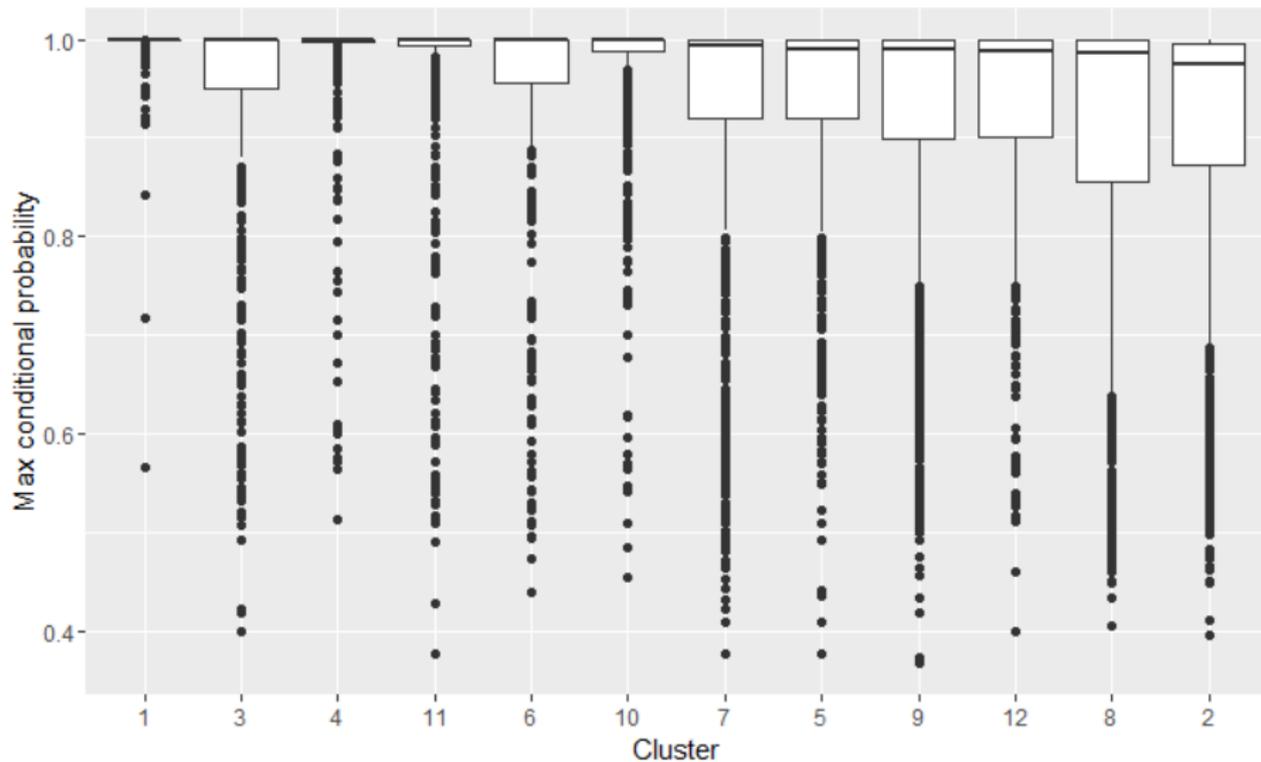
# Examining GMM results



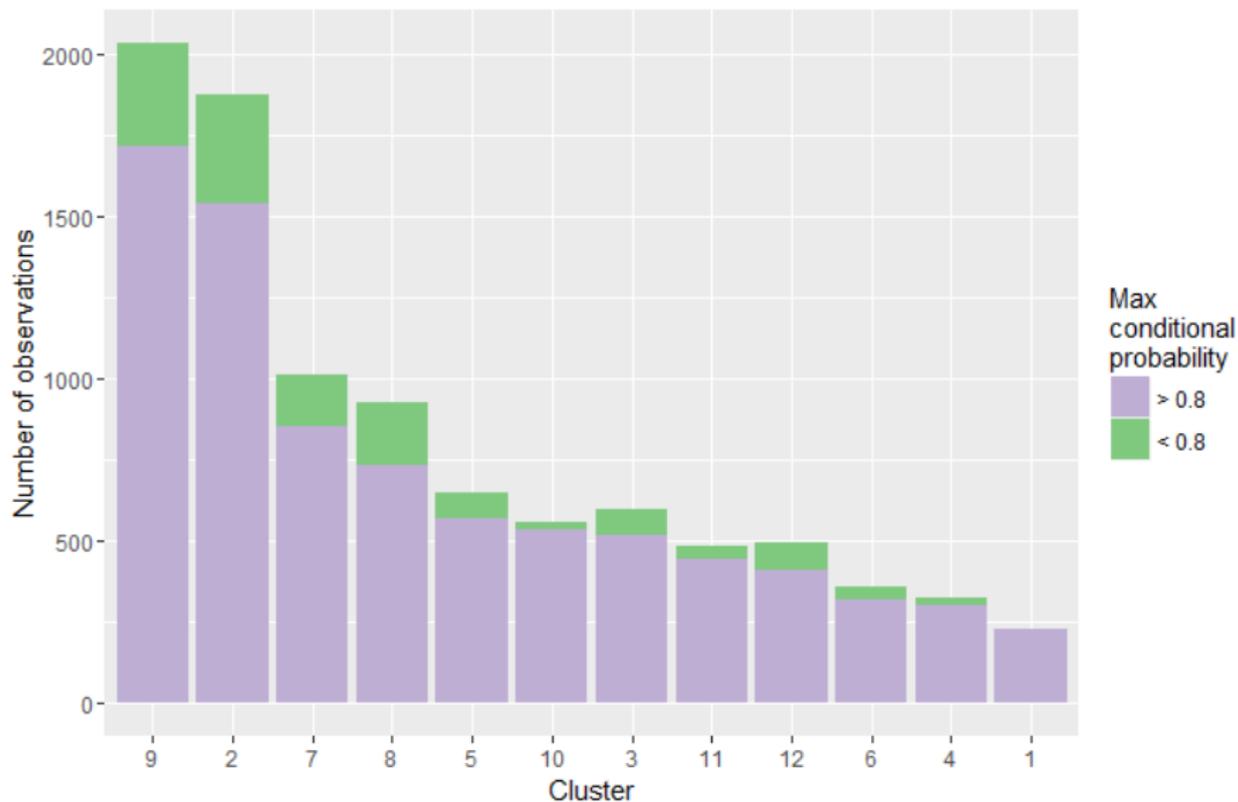
# Evaluation of clustering quality



# Evaluation of clustering quality



# Evaluation of clustering quality



# Conclusions: RNA-seq co-expression

Some practical questions to consider prior to co-expression analyses:

- Should all genes be included?

Screening via differential analysis or a filtering step (based on mean expression or coefficient of variation)...

↪ Usually a good idea, genes that contribute noise will affect results!

- What to do about replicates?

Average, or model each one independently?

↪ Note that the PMM makes use of experimental condition labels, but the GMM does not...

## A note about **evaluating** clustering approaches<sup>8</sup>

- Clustering results can be evaluated based on internal criteria (e.g., statistical properties of clusters) or external criteria (e.g., functional annotations)
- Preprocessing details (normalization, filtering, dealing with missing values) can affect clustering outcome
- Methods that give different results depending on the initialization should be rerun multiple times to check for stability
- Most clustering methods will find clusters even when no actual structure is present  $\Rightarrow$  good idea to compare to results with randomized data!

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<sup>8</sup>D'haeseller, 2005

# A note about validating clustering approaches on real data

- Difficult to compare several clustering algorithms on a given dataset (and difficult to discern under which circumstances a particular method should be preferred)
  - **Adjusted Rand index**: measure of similarity between two data clusterings, adjusted for the chance grouping of elements
    - ↪ ARI has expected value of 0 in the case of a random partition, and is bounded above by 1 in the case of perfect agreement

# A note about validating clustering approaches on real data

- Difficult to compare several clustering algorithms on a given dataset (and difficult to discern under which circumstances a particular method should be preferred)
  - **Adjusted Rand index**: measure of similarity between two data clusterings, adjusted for the chance grouping of elements
    - ↪ ARI has expected value of 0 in the case of a random partition, and is bounded above by 1 in the case of perfect agreement
- Difficult to evaluate how well a given clustering algorithm performs on transcriptomic data
- No one-size-fits-all solution to clustering, and no consensus of what a “good” clustering looks like  $\Rightarrow$  use more than one clustering algorithm!

## Final thoughts<sup>9</sup>

“

There is no single best criterion for obtaining a partition because no precise and workable definition of *cluster* exists. Clusters can be of any arbitrary shapes and sizes in a multidimensional pattern space. Each clustering criterion imposes a certain structure on the data, and if the data happen to conform to the requirements of a particular criterion, the true clusters are recovered.

”

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<sup>9</sup> Jain & Dubes, 1988

# Acknowledgements & References



## MixStatSeq ANR-JCJC grant

Thanks to **Gilles Celeux** (Inria Saclay - Île-de-France), **Cathy Maugis-Rabusseau** (INSA / IMT Toulouse), **Etienne Delannoy**, **Marie-Laure Martin-Magniette** (SPS), and **Panos Papastamoulis** (University of Manchester)

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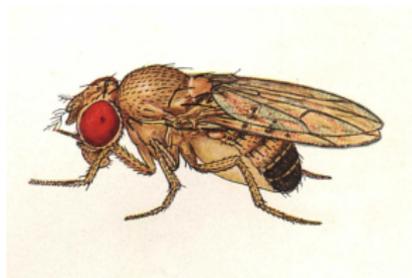
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# Real data analysis: Embryonic fly development

- modENCODE project to provide functional annotation of *Drosophila* (Graveley et al., 2011)
- Expression dynamics over 27 distinct stages of development during life cycle studied with RNA-seq
- 12 embryonic samples (collected at 2-hr intervals over 24 hrs) for 13,164 genes downloaded from ReCount database (Frazee et al., 2011)



# Real data analysis: Embryonic fly development

- Screen genes to include only DE genes (DESeq2)
- K-means clustering
- Hierarchical clustering
- Gaussian mixture model on transformed normalized expression profiles

Keep in mind the advantages / disadvantages of different approaches: speed, stability, robustness, interpretability, model selection, ...